

## RANDOM NUMBER GENERATOR FOR THE COMMAND LINE RG 0.4.2 BETA

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### 1. PROPER USE OF THE GENERATOR TO PRESERVE ITS INTERNAL INTEGRITY

When executed repeatedly from the command line or a script, rg preserves the integrity of its internal random number generator via the option -I (capital i). Generating N random numbers using the -N option is thus the same as calling rg N times with the -I option.

The generator returns a single line of output. It consists of a space-separated list of random numbers, followed by ':' and a comma-separated list of shuffle table values that are to be used with the -I option during the next call.

```
#!/bin/bash
# The initialization option -I is a capital i, not a small ell.

# Initialization of rg
nextlnit='rg -S 0 | awk -F' : ' '{print $2}''

# Random values in a single variable
out='rg -I $nextlnit -N 6 -D Exponential -m 5'
randomValues='echo $out | awk -F' : ' '{print $1}''
nextlnit='echo $out | awk -F' : ' '{print $2}''

# do something with the random numbers
echo Random values in a single variable
for value in $randomValues; do
    echo $value
done

# Random values in an array – note the () for randomValues
out='rg -I $nextlnit -N 5 -D Pareto -k 83456 -b 1.1'
randomValues=('echo $out | awk -F' : ' '{print $1}''')
nextlnit='echo $out | awk -F' : ' '{print $2}''

# do something with the random numbers
numberOfValues=${#randomValues[@]}
echo ""; echo Random values in an array
for (( i=0; i<$numberOfValues; i++ )); do
    echo ${randomValues[$i]}
done
```

# Usage of rg

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## Usage:

```
rg -S seed | -I initialization_vector [-N sample_size]
    [-D distribution_name] [-m mu] [-l lambda] ...
    [-E | -F | -A] [-O output_format] [-V] [-Q]
```

`rg` generates a sample of pseudo random numbers. It supports the following distributions: Uniform on (0,1), Exponential, Erlang, Gamma, Normal, Lognormal, Weibull, Pareto, Geometric, and Poisson.

When executed repeatedly from the command line, `rg` preserves the integrity of the internal generator via the option `-I`. Generating `N` random numbers using the `-N` option is thus the same as calling `rg` `N` times with the `-I` option.

## Parameters

- S** - seed of the generator. A non-negative integer value.
- I** - initialization (capital I) of the generator. The argument is a comma-separated list of shuffle table values that were returned with random numbers generated during the previous call.
- N** - the size of the generated random sample
- D** - the desired probability distribution; one of: Uniform, Exponential, Erlang, Gamma, Normal, Lognormal, Weibull, Pareto, Poisson
- m** - mu (it is the mean for the Exponential, Poisson, and Normal distributions)
- l** - the rate parameter lambda (small e11) of the Exponential and Erlang distribution
- s** - sigma squared - the variance of the (underlying) Normal distribution
- a** - the shape parameter alpha of the Gamma and Weibull distribution
- b** - the scale parameter beta of the Gamma and Weibull distribution, the shape parameter beta of the Pareto distribution
- k** - the scale parameter (minimum) of the Pareto distribution, or the shape parameter of the Erlang distribution
- p** - the probability of success for the Geometric distribution
- E** - engineering (fixed-point) output format, with C's default number of significant digits (%e). For continuous distributions only.
- F** - floating-point output format, with C's default number of significant digits (%f). For continuous distributions only.
- A** - automatic output format - preserve as many significant digits as possible, using the '%e' or '%f' format as necessary (%.30g). For continuous distributions only.
- O** - specify the output format as for printf in C. E.g. '%.6g'. For continuous distributions only.
- V** - verbose output to stderr, including the version of the generator
- Q** - quiet output (suppress output of initialization vector)

## Returns

Space-separated list of random numbers, followed by ':' and a comma-separated list of shuffle table values that are to be used with the `-I` option during the next call.

## Version

0.4.2 beta

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## 2. SUPPORTED DISCRETE DISTRIBUTIONS AND THEIR PARAMETERS

In the following sections  $X$  will denote a random variable with the discussed distribution.

### 2.1. Geometric Distribution.

$$X \sim \text{Geom}(p) \quad \text{if} \quad P(X = k) = p(1 - p)^k \quad \text{for } k = 1, 2, 3, \dots$$

where  $0 < p \leq 1$ . The variable  $X$  can be viewed as the index of the first successful trial in a sequence of independent Bernoulli trials with probability of success equal to  $p$ . We often think of waiting for the first Head in repeated independent coin tosses with  $P(\text{Head}) = p$ . Then  $X$  is the toss number of the first Head.

Geometric distribution is closely related to the exponential distribution, which is often used to model a continuous random waiting time for the next customer. Geometric distribution can be viewed as a discrete version of such waiting time. Both these distributions share many properties, for example they are both memoryless.

```
rg -S <seed> -D Geometric -p <probability>
```

### 2.2. Poisson Distribution.

$$X \sim \text{Poisson}(\mu) \quad \text{if} \quad P(X = k) = \frac{e^{-\mu} \mu^k}{k!} \quad \text{for } k = 0, 1, 2, 3, \dots$$

where  $\mu > 0$  is the mean of  $X$ , i.e.  $EX = \mu$ .

```
rg -S <seed> -D Poisson -m <mu>
```

## 3. SUPPORTED CONTINUOUS DISTRIBUTIONS AND THEIR PARAMETERS

In the following sections  $X$  will denote a random variable with the discussed distribution, and  $f(x)$  will represent its probability density function (pdf).

**3.1. Continuous Uniform Distribution.** In general, the distribution is uniform over an interval  $[a, b]$ , but only Uniform(0,1) is implemented so far. This is the default distribution.

```
rg -S <seed>
rg -S <seed> -D Uniform -a <minimum> -b <maximum>
```

### 3.2. Exponential Distribution.

$$X \sim \text{Exp}(\lambda) \quad \text{if its pdf is} \quad f(x) = \begin{cases} \lambda e^{-\lambda x} & x \geq 0 \\ 0 & \text{otherwise,} \end{cases}$$

where  $\lambda > 0$  is the rate parameter. The expectation (mean) of  $X$  is  $EX = \mu = 1/\lambda$ .

Exponential distribution is often used to model a continuous random waiting time for the next customer. A related distribution is the geometric distribution. It can be viewed as a discrete version of such waiting time. Both these distributions share many properties, for example they are both memoryless.

```
rg -S <seed> -D Exponential -l <lambda>
rg -S <seed> -D Exponential -m <mean>
```

### 3.3. Erlang Distribution.

$$X \sim \text{Erlang}(k, \lambda) \quad \text{if its pdf is} \quad f(x) = \begin{cases} \frac{1}{(k-1)!} \lambda^k x^{k-1} e^{-\lambda x} & x \geq 0 \\ 0 & \text{otherwise,} \end{cases}$$

where  $k \in \mathbb{N}^+$  (a positive integer) is the shape parameter, and  $\lambda > 0$  is the rate parameter. The sum of  $k$  independent  $\text{Exp}(\lambda)$  random variables has the  $\text{Erlang}(k, \lambda)$  distribution.

```
rg -S <seed> -D Erlang -k <shape> -l <lambda>
```

### 3.4. Gamma Distribution.

$$X \sim \text{Gamma}(\alpha, \beta) \quad \text{if its pdf is} \quad f(x) = \begin{cases} \frac{1}{\Gamma(\alpha)} \beta^{-\alpha} x^{\alpha-1} e^{-x/\beta} & x \geq 0 \\ 0 & \text{otherwise,} \end{cases}$$

where  $\alpha > 0$  is the shape parameter, and  $\beta > 0$  is the scale parameter. The expectation of  $X$  is  $EX = \alpha\beta$ . If  $\alpha$  is an integer, then the  $\text{Gamma}(\alpha, \beta)$  distribution is the same as the  $\text{Erlang}(k = \alpha, \lambda = 1/\beta)$  distribution. Notice the inverse of the scale parameter.

Caution, sometimes the Gamma distribution is defined with the scale parameter  $1/\beta$  as in the Erlang distribution. Make sure that you use the correct scale parameter! If you cannot verify the form of the pdf, you can use the expectation  $EX = \alpha\beta$  if its value is known. Then the scale parameter to use with the `rg` generator is  $\beta = EX/\alpha$ .

```
rg -S <seed> -D Gamma -a <alpha> -b <beta>
```

**3.5. Normal Distribution (Gaussian Distribution).**

$$X \sim N(\mu, \sigma^2) \quad \text{if its pdf is} \quad f(x) = \frac{1}{\sqrt{2\pi} \sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

where  $\mu$  is the mean, and  $\sigma^2 > 0$  is the variance of the distribution. Caution, some books use the standard deviation  $\sigma$  instead of the variance  $\sigma^2$  in the normal distribution notation. Make sure that you use the variance  $\sigma^2$  with `rg`!

```
rg -S <seed> -D Normal -m <mu> -s <sigma_squared>
```

**3.6. Lognormal Distribution.**

$$X \sim \text{Ln } N(\mu, \sigma^2) \quad \text{if} \quad \ln(X) \sim N(\mu, \sigma^2).$$

The parameters  $\mu$  and  $\sigma^2 > 0$  are the mean and variance, respectively, of the *underlying normal* distribution. Caution, some books use the standard deviation  $\sigma$  instead of the variance  $\sigma^2$  in the normal distribution notation. Make sure that you use the variance  $\sigma^2$  with `rg`!

```
rg -S <seed> -D Lognormal -m <mu> -s <sigma_squared>
```

**3.7. Weibull Distribution.**

$$X \sim \text{Weibull}(\alpha, \beta) \quad \text{if its pdf is} \quad f(x) = \begin{cases} \frac{\alpha}{\beta} \left(\frac{x}{\beta}\right)^{\alpha-1} e^{-(x/\beta)^\alpha} & x \geq 0 \\ 0 & \text{otherwise,} \end{cases}$$

where  $\alpha > 0$  is the shape parameter, and  $\beta > 0$  is the scale parameter.

```
rg -S <seed> -D Weibull -a <alpha> -b <beta>
```

**3.8. Pareto Distribution.**

$$X \sim \text{Pareto}(k, \beta) \quad \text{if its pdf is} \quad f(x) = \begin{cases} \beta k^\beta x^{-(\beta+1)} & x \geq k \\ 0 & \text{otherwise,} \end{cases}$$

where  $k > 0$  is the scale parameter, and  $\beta > 0$  is the shape parameter. The parameter  $k$  is the minimal possible value of  $X$ . The parameter  $\beta$  is sometimes called the tail index.

```
rg -S <seed> -D Pareto -k <minimal_value> -b <beta>
```